

Percentage**Lecture sheet – 1**

- ***What is percentage?***

→ In mathematics, a percentage is a number or ratio expressed as a fraction of 100. It is denoted using the percent sign “%”.

Example:

$$1 \% = \frac{1}{100} \quad , \quad 15 \% = \frac{15}{100} \quad , \quad 137\% = \frac{137}{100}$$

- **$100 \% = \frac{100}{100} = 1$**

- ***Express the following quantities in fractions and decimals.***

1) 60 % 2) 125 %

Solution:

$$\begin{aligned} 1) \ 60 \% &= \frac{60}{100} \\ &= \frac{3}{5} \quad \text{[Reducing]} \end{aligned}$$

$$60 \% = \frac{3}{5}$$

Again,

$$60 \% = \frac{60}{100}$$

= 0.6 [When dividing any number by 10,100, the decimal point moves to the left as many as the number of 0s]

$$60 \% = 0.6$$

$$2) 125 \%$$

$$= \frac{125}{100}$$

$$= \frac{5}{4}$$

$$= 1 \frac{1}{4}$$

$$125 \% = 1 \frac{1}{4}$$

Again,

$$125 \%$$

$$= \frac{125}{100}$$

$$= 1.25$$

$$125 \% = 1.25$$

1) Exercise (Do yourself):

*** Express the following quantities in fractions and decimals:**

$$\text{a) } 34 \% \quad \text{b) } 89 \% \quad \text{c) } 25 \% \quad \text{d) } 42 \%$$

*** Express the following fractions and decimals by using percentage symbol %:**

Solution:

$$1) \frac{24}{100} = 24\% \left[\frac{1}{100} = \% \right]$$

$$2) 0.03 = \frac{3}{100} = 3\%$$

$$3) \frac{23}{20} = \frac{23 \times 5}{20 \times 5} = \frac{115}{100} = 115\%$$

2) Exercise (Do yourself):

* Express the following fraction and decimals by using the percent symbol % :

a) 0.54 b) $\frac{21}{50}$ c) 0.3 d) $\frac{12}{25}$

* *Fill in the blanks:*

1. 25 litres are _____ % of 50 litres.
2. _____ kilograms are 20% of 120 kilogram.
3. 16 people are 32% of _____ people.

Solution:

1. 25 litres are 50 % of 50 litres.

Rough

$$25 = \square \% \text{ of } 50$$

$$\rightarrow 25 = \frac{\square}{100} \times 50 \quad [\% = \frac{1}{100} \text{ and 'of' } = \times \text{ (multiplication)}]$$

$$\rightarrow 25 = \frac{\square \times 50}{100}$$

$$\rightarrow 25 = \frac{\square}{2}$$

$$\rightarrow 25 \times 2 = \square$$

$$\rightarrow \square = 50$$

2) 24 kilograms are 20 % of 120 kilograms.

Rough

$$\square = 20 \% \text{ of } 120$$

$$\rightarrow \square = \frac{20}{100} \times 120$$

$$\rightarrow \square = \frac{20 \times 120}{100}$$

$$\rightarrow \square = 2 \times 12$$

$$\rightarrow \square = 24$$

3) 16 people are 32% of 50 people.

Rough

$$16 = 32 \% \text{ of } \square$$

$$\rightarrow 16 = \frac{32}{100} \times \square$$

$$\rightarrow 16 = \frac{32 \times \square}{100}$$

$$\rightarrow 16 \times 100 = 32 \times \square$$

$$\rightarrow 1600 = 32 \times \square$$

$$\rightarrow \frac{1600}{32} = \square$$

$$\rightarrow 50 = \square$$

$$\rightarrow \square = 50$$

3) *Exercise (Do yourself):*

* Fill in the blanks:

- a) 12 people is _____ % of 20 people.
- b) 150 % of 300 Taka is _____ Taka.
- c) 56 % of _____ grams is 42 grams.